

# Real Keynesian Models and Sticky Prices

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# Introduction : Inflation

- ▶ A set of puzzles in the behaviour of inflation, when observed through the lens of a New Keynesian model
  - × missing inflation
  - × missing deflation
  - × missing volatility of inflation at the ZLB
  - × etc.
- ▶ One way out is to enrich the standard New Keynesian model
- ▶ We suggest an alternative perspective that questions the real side of the model that NK models build on

## Introduction : Demand Shocks

- ▶ In many (most) macro models, “demand” shocks (optimism, positive sentiment, good news, possibly lax credit,...) are expansionary because prices are sticky.
- ▶ Smaller literature suggests that sticky prices may not be necessary for demand shocks to be expansionary.  $\rightsquigarrow$  *Real Keynesian* models
- ▶ If *prices are sticky* (after all), this might be a rather theological distinction.
- ▶ Questions addressed in this paper: should we care that a model is *Real Keynesian*
  1. for our understanding of how monetary shocks affect the economy?
  2. for our understanding of the conduct of monetary policy?
  3. for the explained behaviour of inflation?
- ▶ Answers are yes, yes and yes.

## Introduction: Contributions

- ▶ Propose a new class of simple extensions of the *New Keynesian* model
- ▶ *Real Keynesian* models have very different implications for monetary policy **when prices are sticky**.
- ▶ Show that it is empirically relevant

# Roadmap

1. Theory
2. Empirical Relevance
3. Focus on the Zero Lower Bound and Missing Deflation

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# The Real Structure of the Simplest NK Model

- ▶ No technology shock, no capital, CRS:  $y_t = c_t = l_t$
- ▶ Model with sticky prices:

$$l_t = E_t l_{t+1} - \alpha_r (i_t - E_t \pi_{t+1}) + d_t \quad \text{Euler Equation (EE)}$$

$$\pi_t = \beta E_t \pi_{t+1} + \kappa mc_t \quad \text{Phillips Curve (PC)}$$

- ▶ Marginal cost is assumed to depend on labor market tightness (real wage)  $\rightsquigarrow$   
 $mc_t = \gamma \ell_t$
- ▶ When prices are fully flexible:

$$l_t = E_t l_{t+1} - \alpha_r r_t + d_t \quad \text{Euler Equation (EE)}$$

$$mc_t = 0 = \gamma \ell_t \quad \text{Aggregate Supply (AS)}$$

# The Real Structure of the Simplest NK Model

Flex price NK model :

$$l_t = E_t l_{t+1} - \alpha_r r_t + d_t \quad (\text{EE})$$

$$0 = \gamma \ell_t \quad (\text{AS})$$



# The Real Structure of the Simplest NK Model

i.i.d. case :

$$l_t = -\alpha_r r_t + d_t \quad (\text{EE})$$

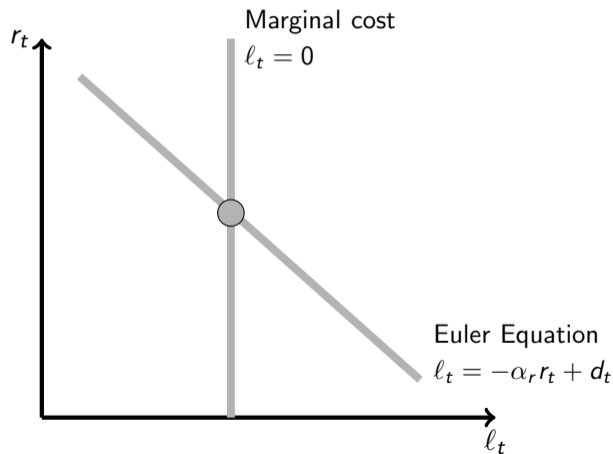
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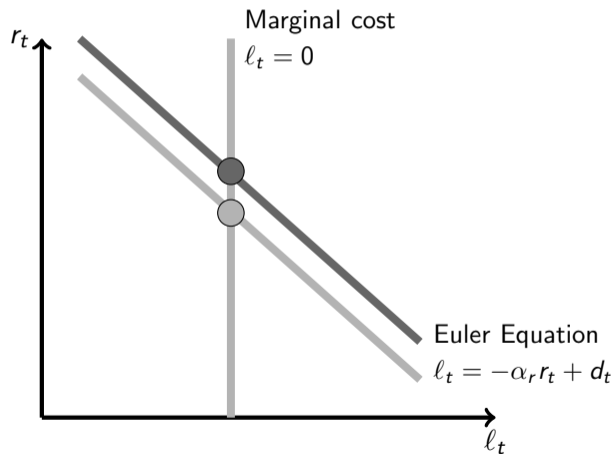


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## Enriching the Real Structure

- ▶ Let's have a more general model in which AS is not infinitely sloped.
- ▶ Assume now that marginal cost also depend on the real interest rate  $r$  (*cost channel*)

$$mc_t = \gamma_{\ell} \ell_t + \gamma_r r_t$$

# Enriching the Real Structure

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- ▶ NK model corresponds to  $\gamma_r = 0$

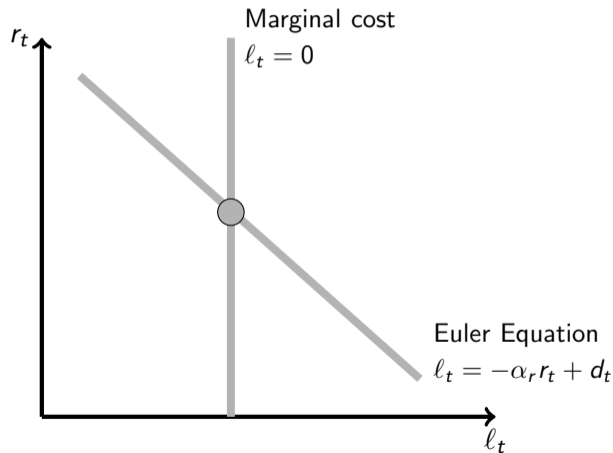
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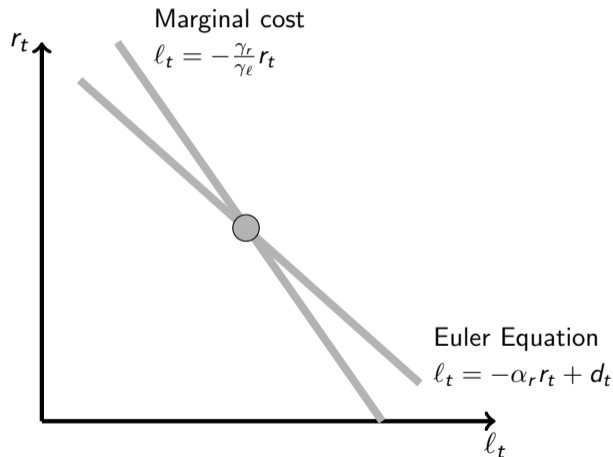
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- ▶ Assume  $\gamma_r$  is small (compared to  $\gamma_\ell$ )





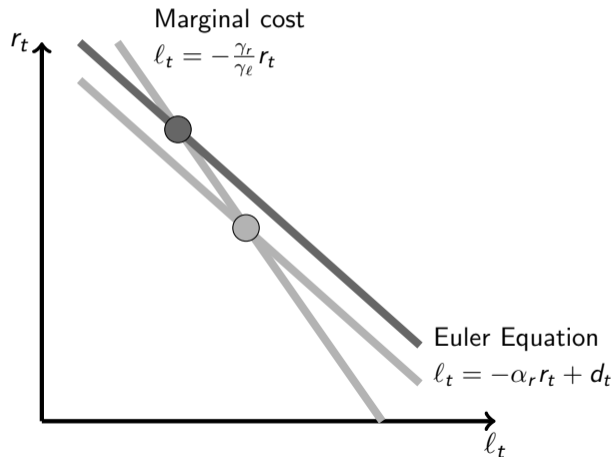
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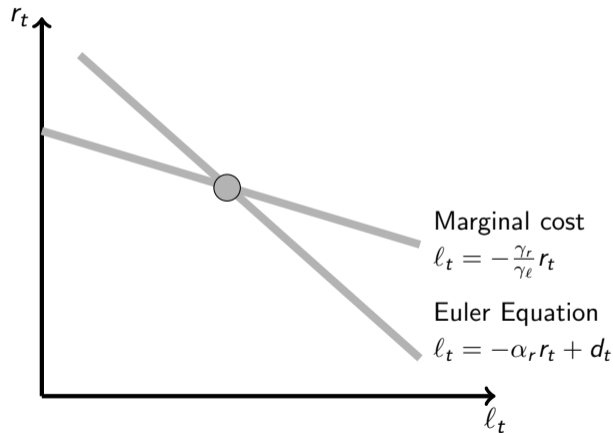
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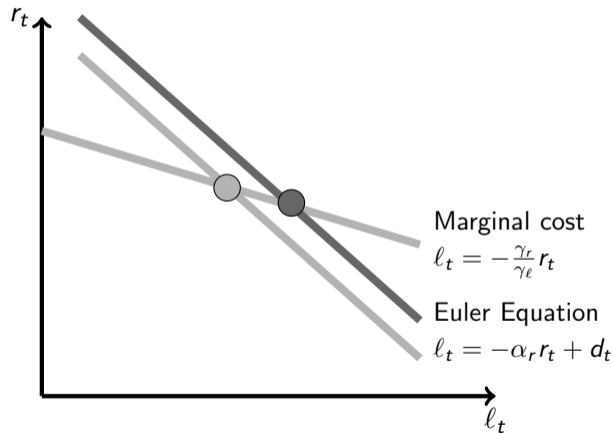
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## Towards An Extended Model

- ▶ Importance of the cost channel:  $\frac{\gamma_r}{\gamma_e} \leq \alpha_r$
- ▶ In the *i.i.d.* case, we say that the model is *Real Keynesian* if  $\frac{\gamma_r}{\gamma_e} > \alpha_r$
- ▶ Need to go beyond the *i.i.d.* case
- ▶  $\rightsquigarrow$  Expectations in the Euler equation will matter

# The RK condition

## Result 1

*With flex. prices, positive demand shocks (both current and expected future) of any persistence have a positive effect on  $\ell$  if and only if*

$$\frac{\gamma_r}{\gamma_\ell} > \frac{\alpha_r}{\alpha_\ell} \quad (RK)$$

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*With flex. prices, positive demand shocks (both current and expected future) of any persistence have a positive effect on  $\ell$  if and only if*

$$\frac{\gamma_r}{\gamma_\ell} > \frac{\alpha_r}{(1 - \alpha_\ell)} \quad (RK)$$

*where the Euler Equation is*

$$\ell_t = \alpha_\ell E_t \ell_{t+1} - \alpha_r (i_t - E_t \pi_{t+1}) + d_t$$

# Extended Sticky Price Linearized Model

$$l_t = \alpha_\ell E_t l_{t+1} - \alpha_r (i_t - E_t \pi_{t+1}) + d_t$$
$$\pi_t = \beta E_t \pi_{t+1} + \kappa (\gamma_\ell l_t + \gamma_r (i_t - E_t \pi_{t+1}))$$

Euler Equation (EE)

Phillips Curve (PC)

- ▶ Two changes (microfoundations in the paper):
  - ×  $\alpha_\ell \leq 1$  : *discounted EE*
  - ×  $\gamma_r \geq 0$  : *cost channel*
- ▶ Nothing novel, except for putting them together.
- ▶ Note: standard NK model:  $\alpha_\ell = 1, \gamma_r = 0$
- ▶ To remember:  $\alpha$ 's for the EE,  $\gamma$ 's for the PC

## Extended Sticky Price Linearized Model

- ▶ with demand, cost-push and monetary policy shocks

$$l_t = \alpha_\ell E_t l_{t+1} - \alpha_r (i_t - E_t \pi_{t+1}) + d_t \quad (\text{EE})$$

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## Extended Sticky Price Linearized Model

- ▶ with demand, cost-push and monetary policy shocks

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$$i_t = E_t \pi_{t+1} + \phi l_t + \nu_t \quad (\text{Policy Rule})$$

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## Theorem 1

For any Taylor rule  $i_t = \tilde{\phi}_\pi \pi_t + \tilde{\phi}_\ell l_t + \tilde{\nu}_t$   
that gives determinacy, there exists a policy rule

$$i_t = E_t[\pi_{t+1}] + \phi_\ell l_t + \nu_t$$

that produces the same allocations, with  $\nu_t = a\mu_t + b\tilde{\nu}_t$

# Policy Rules

## Corollary 1

*If monetary policy is given by*

$$i_t = E_t[\pi_{t+1}] + \phi_\ell \ell_t + \phi_\mu \mu_t + \nu_t$$

*with  $\phi_\ell > 0$ , then there is a unique stationary equilibrium.*

# Irrelevance Result

## Result 2

*With sticky prices, RK and NK configurations are not qualitatively distinguishable for demand and markup shocks.*

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i.i.d. case ( $i_t = r_t$ ) :

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$$\pi_t = \kappa(\gamma_\ell \ell_t + \gamma_r r_t) + \mu_t \quad (\text{PC})$$

$$r_t = \phi_\ell \ell_t + \phi_\mu \mu_t + \nu_t \quad (\text{Policy Rule})$$

# Irrelevance Result

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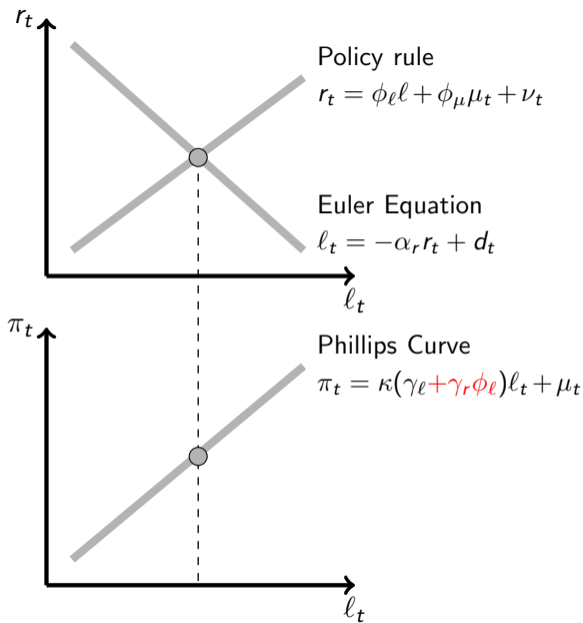
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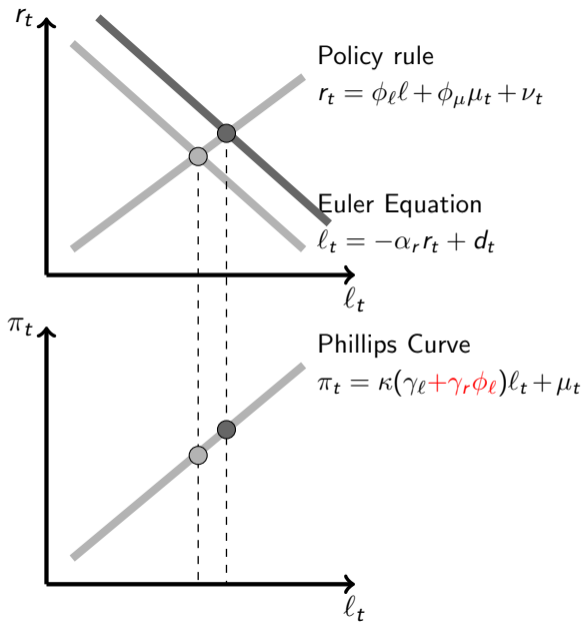
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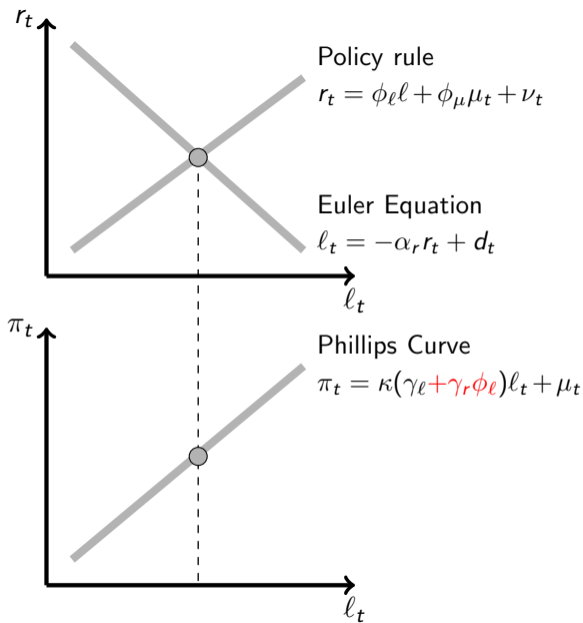
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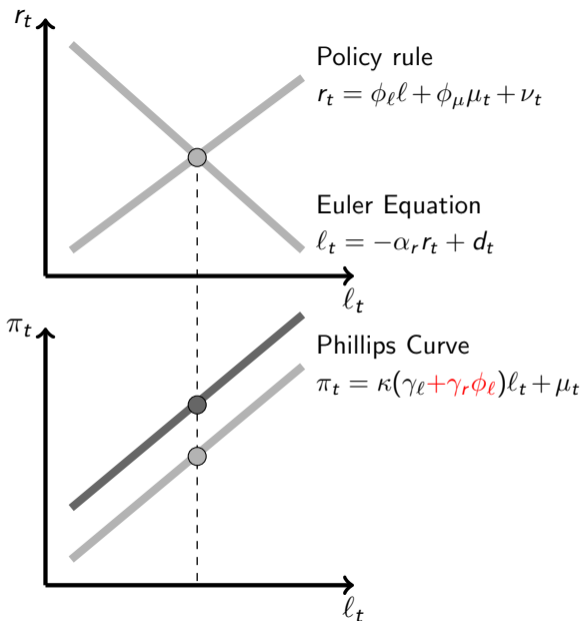
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# RK Matters for Monetary Policy and Monetary Shocks

- ▶ Monetary Policy and Stabilization
- ▶ Determinacy under  $i$  peg
- ▶ Monetary Shocks

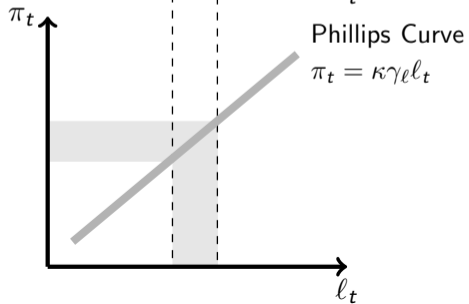
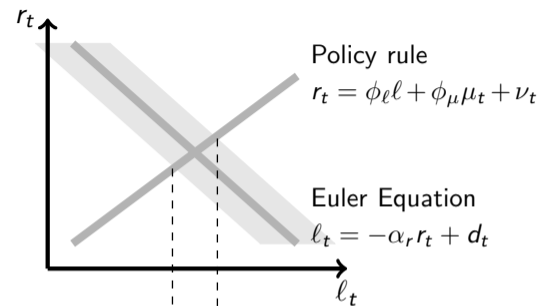
## Effects of Stabilization with Demand Shocks

$$i_t = E_t \pi_{t+1} + \phi_\ell \ell_t + \phi_\mu \mu_t + \nu_t$$

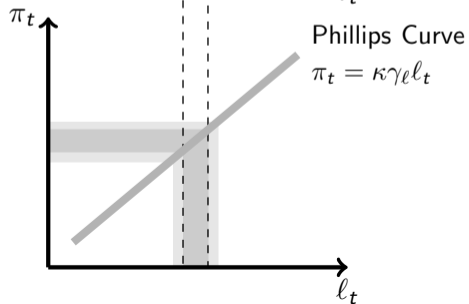
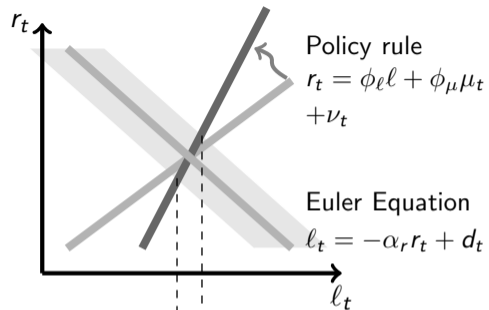
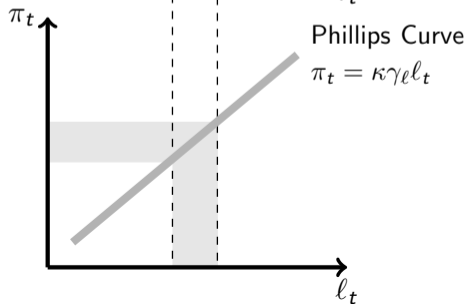
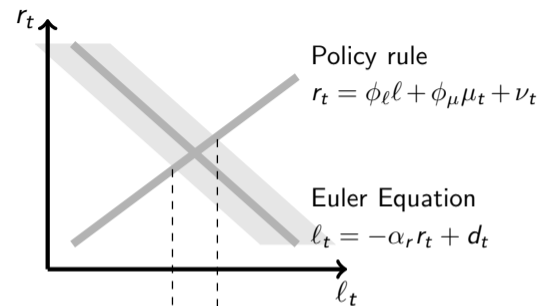
### Result 3

*A more aggressive policy ( $\phi_\ell$  larger) always decreases  $\sigma_\ell^2$  at the cost of increasing  $\sigma_\pi^2$  iff the RK condition is satisfied.*

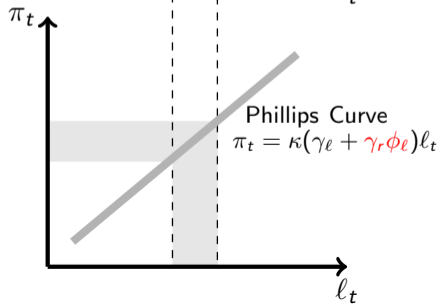
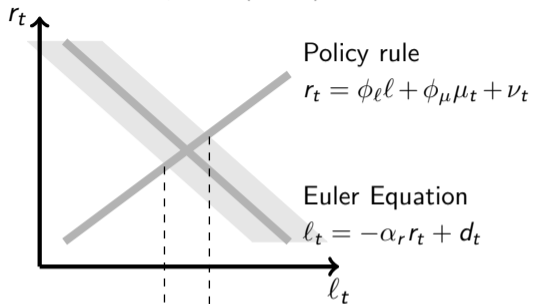
# NK Configuration ( $\gamma_r = 0, \alpha_\ell = 1$ )



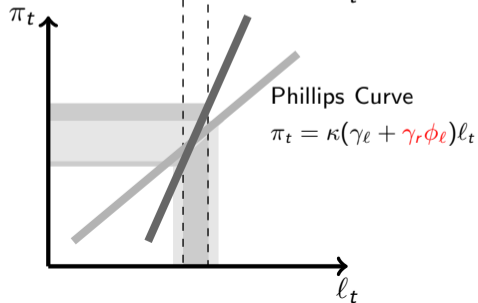
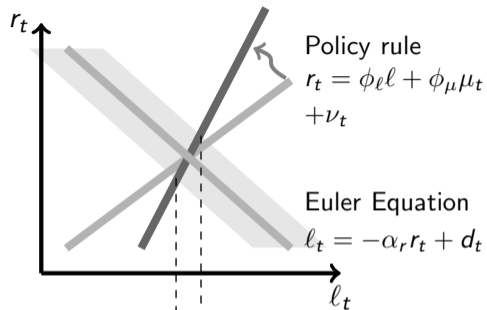
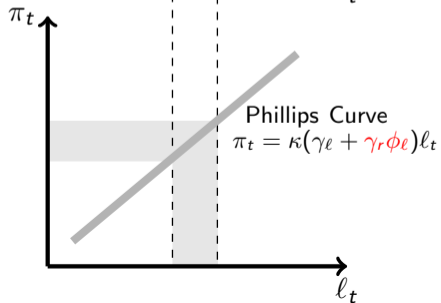
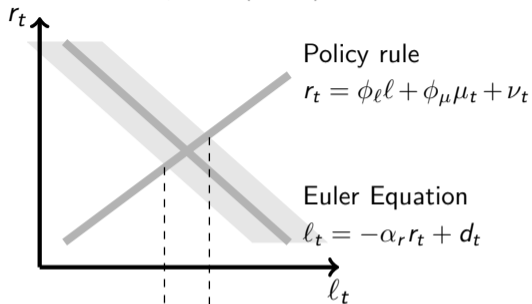
# NK Configuration ( $\gamma_r = 0, \alpha_\ell = 1$ )



Under RK  $\left(\frac{\gamma_r}{\gamma_l} > \frac{\alpha_r}{(1-\alpha_l)}\right)$



Under RK ( $\frac{\gamma_r}{\gamma_l} > \frac{\alpha_r}{(1-\alpha_l)}$ )



## Nominal Interest Rate Peg (ZLB)

- ▶ Suppose policy goes from

$$i_t = E_t \pi_{t+1} + \phi_\ell \ell_t + \phi_\mu \mu_t + \nu_t$$

to

$$i_t = 0.$$

### Result 4

*In the NK configuration,*

- × *indeterminacy*
- × *in all equilibria,  $\sigma_\ell^2$  and  $\sigma_\pi^2$  move together (conditional on demand shocks)*

*In the RK configuration,*

- × *determinacy*
- ×  *$\sigma_\ell^2$  increases but  $\sigma_\pi^2$  decreases (conditional on demand shocks)*



# Monetary Shocks

## Result 5

*In response to a contractionary monetary shocks,*

- ▶ *If the shock is not very persistent, then NK and RK cannot be distinguished.*
- ▶ *If shock is sufficiently persistent,*
  - × *it increases inflation in RK case (neo-Fisherian effect)*
  - × *it decreases inflation in the NK case*
  
- ▶ RK favoured if we observe both (i) persistent monetary shock that (ii) do not lead to a fall in inflation
- ▶ “Congressman Wright Patman effect” (1970) : raising interest rates to fight inflation is like “throwing gasoline on fire”

# Roadmap

1. Theory
2. Empirical Relevance
3. Focus on the Zero Lower Bound and Missing Deflation

# Empirical Relevance

## Phillips Curve Estimates

$$\pi_t = \gamma_f E_t \pi_{t+1} + \kappa \gamma_l \ell_t + \kappa \gamma_r (i_t - E_t \pi_{t+1}) + \mu_t$$

# Empirical Relevance

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$$\pi_t = \gamma_f E_t \pi_{t+1} + \gamma_l l_t + \gamma_r (i_t - E_t \pi_{t+1}) + \mu_t$$

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## Phillips Curve Estimates

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# Empirical Relevance

## Phillips Curve Estimates

$$\pi_t = \gamma_f \pi_{t+1}^e + \gamma_l x_t + \gamma_r (i_t - \pi_{t+1}^e) + \mu_t$$

# Empirical Relevance

## Phillips Curve Estimates

$$\pi_t = \gamma_f \pi_{t+1}^e + \gamma_l x_t + \gamma_r (i_t - \pi_{t+1}^e) + \mu_t$$

- ▶  $\pi_t$ : Headline CPI
- ▶  $\pi_t^e$ : University of Michigan Survey of Consumers
- ▶  $x_t$ : *minus* Unemployment gap from U.S. Congressional Budget Office

# Empirical Relevance

## Phillips Curve Estimates: Basic

$$\pi_t = \gamma_f \pi_{t+1}^e + \gamma_l x_t + \gamma_r (i_t - \pi_{t+1}^e) + \mu_t$$

	OLS	OLS	IV
$\gamma_f$	1.17***	1.11***	1.10***
$\gamma_l$	0.25***	0.12*	0.01
$\gamma_r$	—	0.24***	0.28***

- × Controlling for oil price,
- ×  $i_t - \pi_{t+1}^e$  is instrumented with 6 lags of ROMER & ROMER shocks and their square ,
- × Sample: 1969Q1-2017Q4,
- × NEWKEY & WEST correction for heteroskedasticity and autocorrelation.

# Empirical Relevance

## Phillips Curve Estimates: Hybrid

$$\pi_t = \gamma_f \pi_{t+1}^e + \gamma_b \pi_{t-1} + \gamma_\ell x_t + \gamma_r (i_t - \pi_{t+1}^e) + \mu_t$$

	OLS	OLS	IV
$\gamma_f$	0.77***	0.88***	0.89***
$\gamma_b$	0.35***	0.22*	0.21***
$\gamma_\ell$	0.12*	0.06	0.02
$\gamma_r$	—	0.18***	0.20***

- × Controlling for oil price,
- ×  $i_t - \pi_{t+1}$  is instrumented with 6 lags of ROMER & ROMER shocks and their square ,
- × Sample: 1969Q1-2017Q4,
- × NEWEY & WEST correction for heteroskedasticity and autocorrelation.

# Empirical Relevance

## Phillips Curve Estimates: Hybrid, Various Samples

$$\pi_t = \gamma_f \pi_{t+1}^e + \gamma_b \pi_{t-1} + \gamma_\ell x_t + \gamma_r (i_t - \pi_{t+1}^e) + \mu_t$$

	1969-2006	1969-1992	1992-2017	1984-2006
$\gamma_f$	0.82***	0.84***	0.79***	0.85***
$\gamma_b$	0.32***	0.34***	-0.03	-0.08
$\gamma_\ell$	-0.06	-0.05	0.08	-0.49***
$\gamma_r$	0.20***	0.25***	0.08	0.40***

- × Controlling for oil price,
- ×  $i_t - \pi_{t+1}$  is instrumented with 6 lags of ROMER & ROMER shocks and their square ,
- × Sample: 1969Q1-2006Q4,
- × NEWKEY & WEST correction for heteroskedasticity and autocorrelation.

# Empirical Relevance

## Phillips Curve Estimates: Hybrid, Instrumenting More Variables

$$\pi_t = \gamma_f \pi_{t+1}^e + \gamma_b \pi_{t-1} + \gamma_\ell x_t + \gamma_r (i_t - \pi_{t+1}^e) + \mu_t$$

Instrumented variables		
	$\{\pi_{t+1}^e, \pi_{t-1}, r_t, x_t\}$	$\{\pi_{t+1}^e, r_t, x_t\}$
$\gamma_f$	1.31***	0.87***
$\gamma_b$	0.26***	0.27***
$\gamma_x$	-0.03	0.20
$\gamma_r$	0.23***	0.16***

- × Controlling for oil price,
- × Instruments are 6 lags of ROMER & ROMER shocks and their square ,
- × NEWKEY & WEST correction for heteroskedasticity and autocorrelation.

# Empirical Relevance

Phillips Curve Estimates: Hybrid, Full Info Rat. Exp.

$$\pi_t = \gamma_f \pi_{t+1} + (1 - \gamma_f) \pi_{t-1} + \gamma_l x_t + \gamma_r (i_t - \pi_{t+1}) + \mu_t$$

	x: Labor Share			x: Unempl. gap		
	(1)	(2)	(3)	(4)	(5)	(6)
$\gamma_f$	0.66***	0.66***	0.56***	0.57***	0.61***	0.60***
$\gamma_b$	$1 - \gamma_f$	$1 - \gamma_f$	$1 - \gamma_f$	$1 - \gamma_f$	$1 - \gamma_f$	$1 - \gamma_f$
$\gamma_l$	4.72**	-3.38	-10.12	-0.01	-0.03	-0.09
$\gamma_r$	-	0.18***	0.15***	-	0.17***	0.12**

- × Controlling for oil price,
- × Instruments are: (1), (2), (4) and (5): GALÍ & GERLER's instruments, (3) and (6): 6 lags of ROMER & ROMER shocks and their square, '
- × Sample: 1969Q1-2006Q4,
- × NEWEY & WEST correction for heteroskedasticity and autocorrelation.

# Empirical Relevance

## Phillips Curve Estimates: Recap

- ▶ Recap: The effect of the real interest rate on inflation can be
  - × indirect, through its impact on the gap
  - × direct, on top of the effect of the gap
- ▶ Very strong evidence of the direct effect, not much of the indirect one.
- ▶ Results are (by and large) robust to
  - × various measures of the gap
  - × various measures of the inflation rate
  - × Choice of instruments



# Empirical Relevance

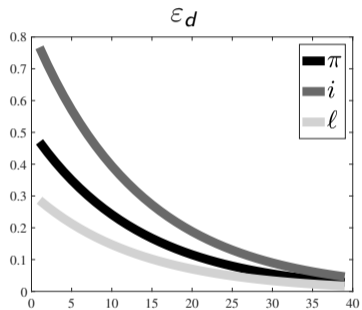
## Full Information

- ▶ Here we estimate the full model by Maximum Likelihood
- ▶ Data:
  - ×  $\pi$ : GDP deflator,
  - ×  $i_t$ : fed funds rate,
  - ×  $l_t$ : minus unemployment rate.
- ▶ Sample:
  - × long: 1954:3- 2007:4,
  - × post-Volker-deflation sample: 1983:4-2007:4
- ▶ Maximum Likelihood estimation

## Result 6

*Estimation shows that the model is in the Real Keynesian region.*

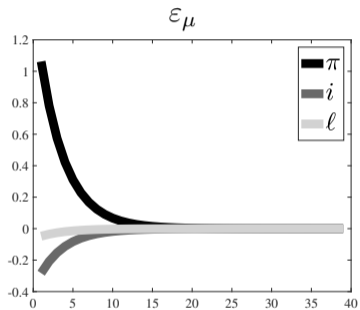
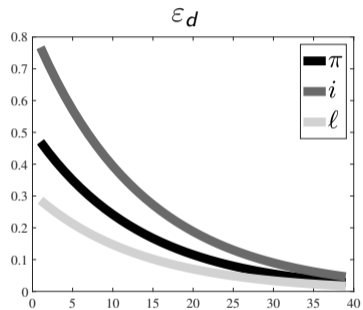
# Max Likelihood Estimation, Full Sample



$\varepsilon_\mu$

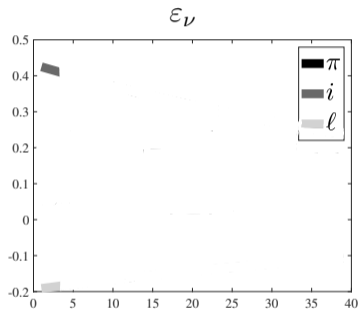
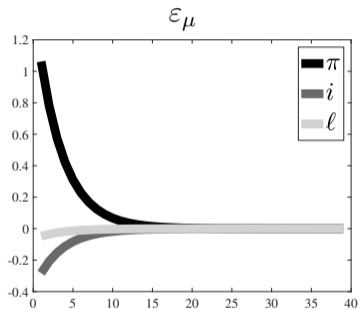
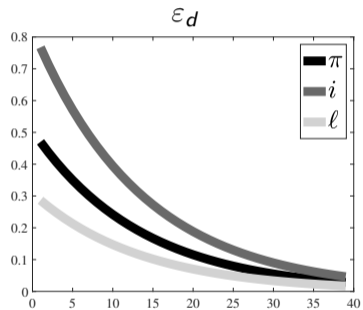
$\varepsilon_\nu$

## Max Likelihood Estimation, Full Sample



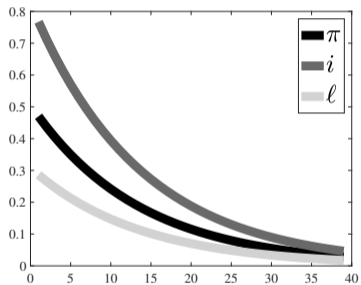
$\varepsilon_\nu$

## Max Likelihood Estimation, Full Sample

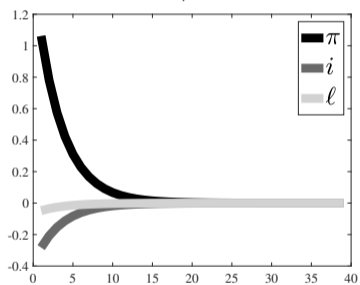


## Max Likelihood Estimation, Full Sample

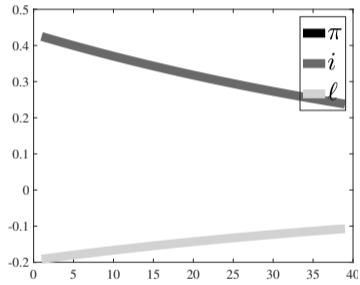
$\varepsilon_d$



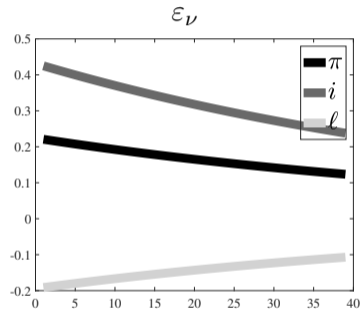
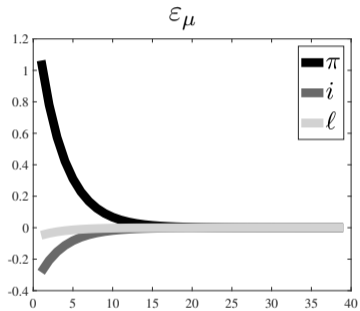
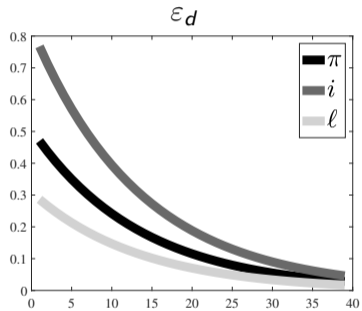
$\varepsilon_\mu$



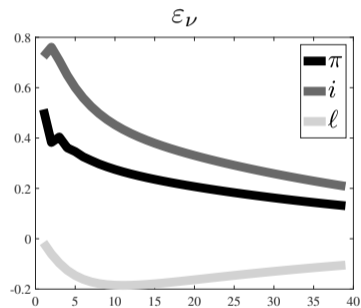
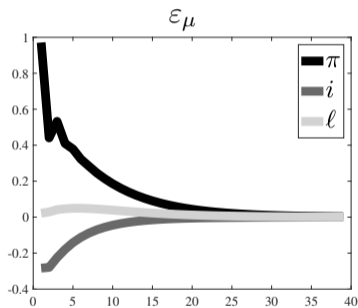
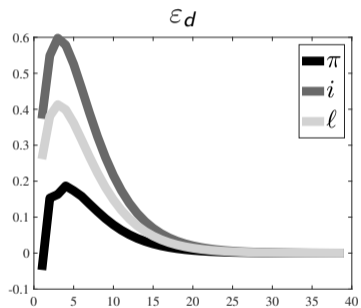
$\varepsilon_\nu$



## Max Likelihood Estimation, Full Sample



Max Likelihood Estimation, Full Sample, Habit persistence, gradual adjustment of  $i$  and hybrid New Phillips curve



# Robustness

- ▶ Results are robust across the 3 following sub-samples
  - I. Pre Volker dis-inflation period (1954:3-1979:1)
  - II. Post Volker dis-inflation period (1983:4-2007:1)
  - III. Zero Lower Bound period (2009:1-2016:3)
- ▶ Results robust when allowing the model to have endogenous propagation (hybrid PC + habit persistence +  $i_{t-1}$  in the policy rule)
- ▶ Results robust when allowing the model to have more shocks
- ▶ Results robust when varying the measure of inflation (CPI or GDP deflator) and of activity (unemployment or hours)



# Roadmap

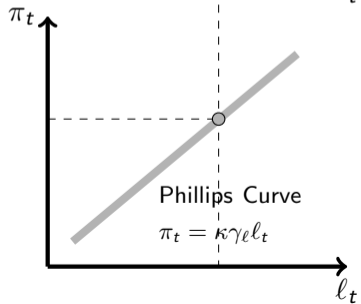
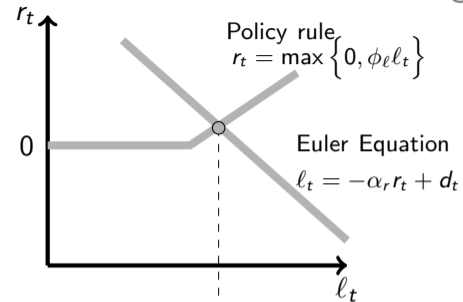
1. Theory
2. Empirical Relevance
3. Focus on the Zero Lower Bound and Missing Deflation

## Low Variance of Inflation at the ZLB

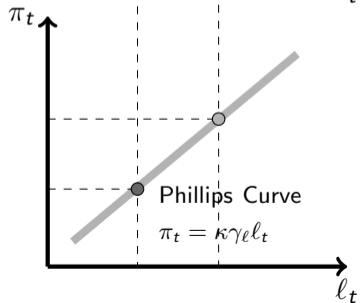
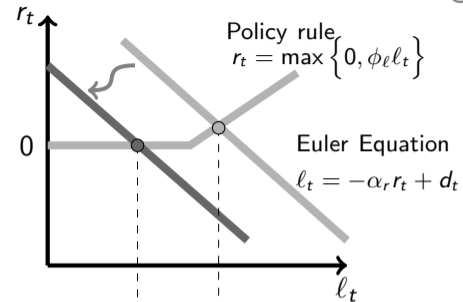
	$\sigma_u$	$\sigma_\pi$	$\sigma_j$
Post-Volcker	: 1.3	.9	2.5
ZLB	: 1.7	.8	.1

- ▶ Observation: the variance of inflation slightly decreased at ZLN.
- ▶ It should have increased in the NK configuration (*under the assumption that demand shocks drove the economy*)
- ▶ But this is consistent with the RK configuration

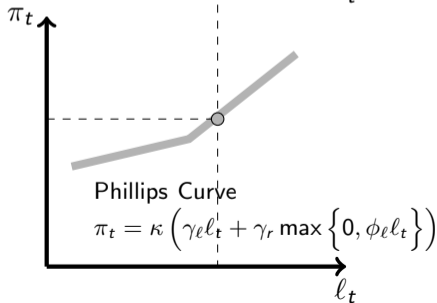
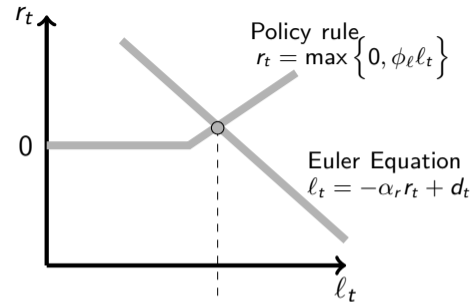
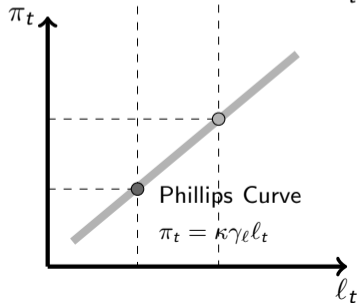
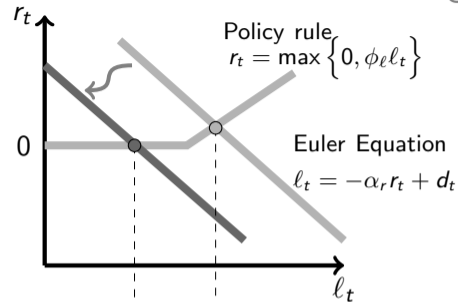
# Zero Lower Bound and Missing Deflation



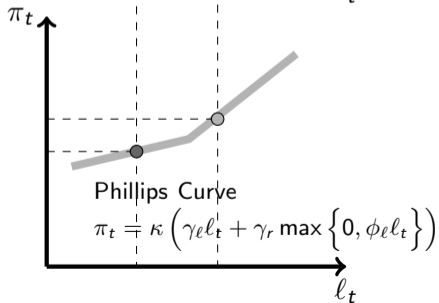
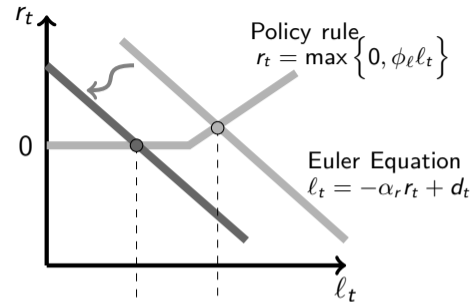
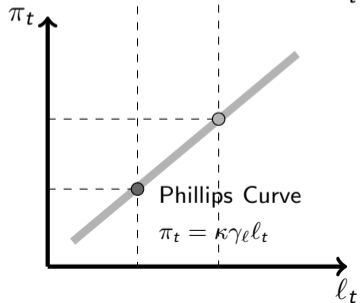
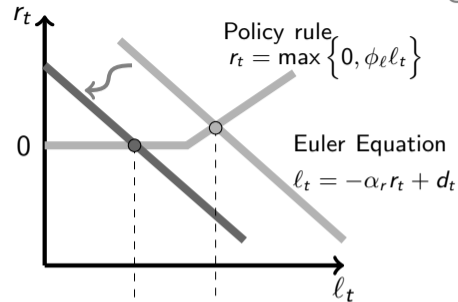
# Zero Lower Bound and Missing Deflation



# Zero Lower Bound and Missing Deflation



# Zero Lower Bound and Missing Deflation



# The ZLB Trap

- ▶ RK framework suggest that ZLB was quasi inevitable following a persistent fall in demand.
- ▶ In RK, both the fall in demand and the response of monetary authorities favours lower inflation:
  - × Initial negative demand shock  $\rightsquigarrow$
  - × Low activity and low inflation  $\rightsquigarrow$
  - × Monetary expansion stimulus  $\rightsquigarrow$
  - × Lower  $i$  and lower inflation  $\rightsquigarrow$
  - × More monetary expansion  $\rightsquigarrow$
  - × Even lower  $i$   $\rightsquigarrow$
  - × Hit the zero lower bound.

# Summary

- ▶ When demand matters with flexible prices (*Real Keynesian* models), adding sticky prices affect the way we think of monetary policy:
  - × trade-off between stabilising inflation and output when facing demand shocks
  - × Determinacy at the ZLB
  - × Variance of inflation and output moving in opposite direction at the ZLB
- ▶ Data favours Phillips Curve with cost channel
- ▶ Data favours *Real Keynesian* configuration
- ▶ Main reason is that monetary shocks are persistent and they have neo-Fisherian effect



